

ECE 101 Lecture #1 Jan 8, 2019  
Introduction to Electronic Circuits

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Textbook\* - eBook (This eBook can be downloaded freely from  
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# CIRCUIT ANALYSIS AND DESIGN

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& Cynthia M. Furse

Ref. C.K. Alexander and M.N.O. Sadiku,  
Fundamentals of Electric Circuits

## CIRCUIT ANALYSIS AND DESIGN

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### Course Grading

- Weekly 15min Quizzes based on Weekly HWs 20%  
(Best 7 out of 9 quizzes  
HWs not collected.)
- Mid-term Examination 30%  
(Feb 7, 1 page of formulas allowed  
in class.)
- Final Examination 50%  
(March 20, 2 pages of formulas allowed)  
8-11 am.

HW #1 issued on Jan 8, 2019  
(to be tested in Quiz #1 on Jan 15)

- [1]. Prob. 1-13 in the eBook
- [2]. Prob. 1-19
- [3]. Prob. 1-25
- [4]. Prob. 1-28
- [5]. Prob. 1-31
- [6]. Prob. 1-40
- [7]. Prob. 1-42
- [8]. Prob. 2-5

In Search of Excellence

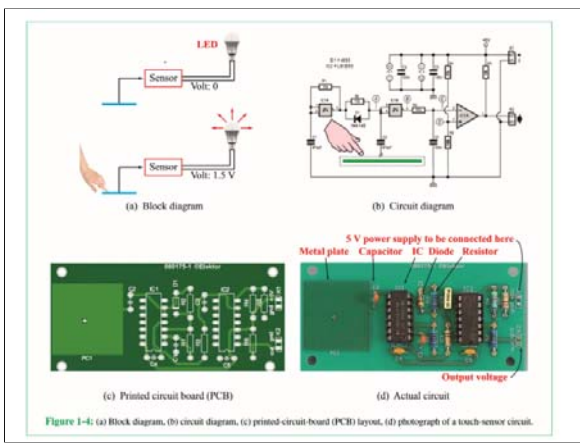
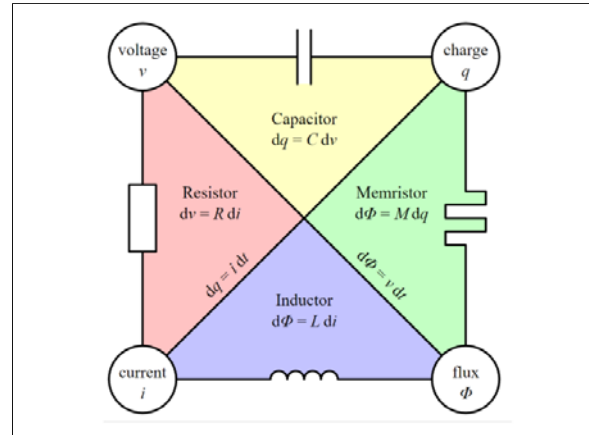
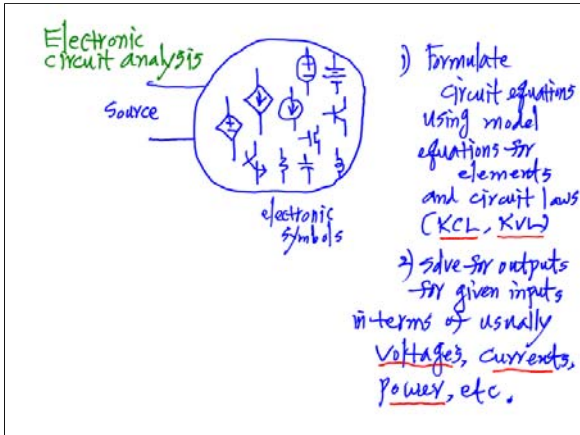
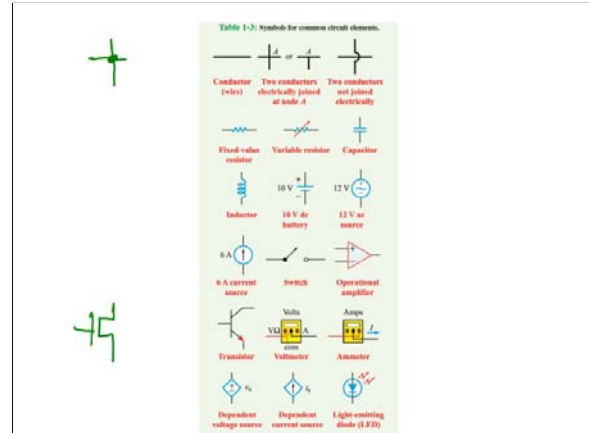


Table 1-2: Multiple and submultiple prefixes.

Prefix	Symbol	Magnitude
exa	E	10 <sup>18</sup>
peta	P	10 <sup>15</sup>
tera	T	10 <sup>12</sup>
giga	G	10 <sup>9</sup>
mega	M	10 <sup>6</sup>
kilo	k	10 <sup>3</sup>
milli	m	10 <sup>-3</sup>
micro	μ	10 <sup>-6</sup>
nano	n	10 <sup>-9</sup>
pico	p	10 <sup>-12</sup>
femto	f	10 <sup>-15</sup>
atto	a	10 <sup>-18</sup>

$V = 9\text{ V}$      $R = 4\ \Omega$   
Ohm

$I = \frac{V}{R} = \frac{9}{4} = 2.25\text{ A}$   
 $p = V \cdot I = 9 \cdot (2.25) = 20.25\text{ W}$

$= \frac{V^2}{R} = \frac{9^2}{4}$   
 $= I^2 R = (2.25)^2 \times 4 = \frac{V^2}{R} = \frac{9^2}{4}$

Switch closes at  $t = 5\text{ s}$

For  $t > 5$ ,  $p_{\text{bulb}} = V_{\text{bulb}} I = \frac{V_{\text{bulb}}^2}{R}$

$I_0 = 2\text{ A}$      $-V_0 + 28 - 10 = 0$   
 $V_0 = 18$

Find the power absorbed in each element (①-⑥)

Element	V	I	Power absorbed
①	30	-5	-150 W
②	12	6	72 W
③	28	2	56 W
④	28	1	28 W
⑤	18	3	54 W
⑥	-10	3	-30 W

-210 W  
 +210 W  
 0

Figure P1.37: Circuit for Problem 1.37.

1.37 Apply the law of conservation of power to determine the amount of power delivered to device 4 in the circuit of Fig. P1.37, given that the amounts of power delivered to the other devices are:  $p_1 = -100\text{ W}$ ,  $p_2 = 30\text{ W}$ ,  $p_3 = 22\text{ W}$ ,  $p_5 = 67\text{ W}$ ,  $p_6 = -201\text{ W}$ , and  $p_7 = 120\text{ W}$ .

### 2.1 OHM'S LAW Resistors

Figure 2-2: Various types of resistors. Rotatable-dial resistors usually are color-coded by 4-, 5-, or 6-band systems.

**Table 2-3: Common resistor terminology.**

<b>Thermistor</b>	$R$ sensitive to temperature
<b>Piezoresistor</b>	$R$ sensitive to pressure
<b>Light-dependent <math>R</math> (LDR)</b>	$R$ sensitive to light intensity
<b>Rheostat</b>	2-terminal variable resistor
<b>Potentiometer</b>	3-terminal variable resistor

### 2-1.2 $i-v$ Characteristics of Ideal Resistor

Based on the results of his experiments on the nature of conduction in circuits, German physicist Georg Simon Ohm (1787–1854) formulated in 1826 the  $i-v$  relationship for a resistor, which has become known as *Ohm's law*. He discovered that the voltage  $v$  across a resistor is directly proportional to the current  $i$  flowing through it, namely

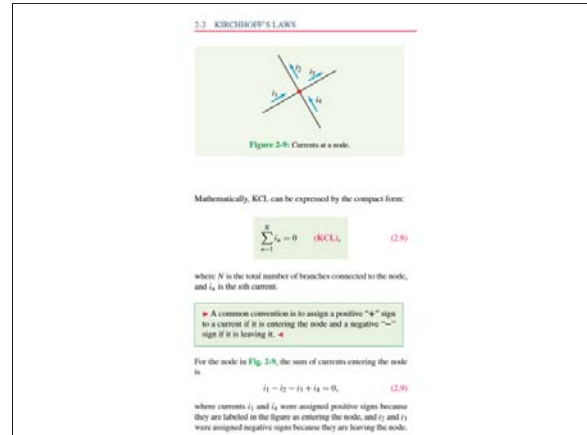
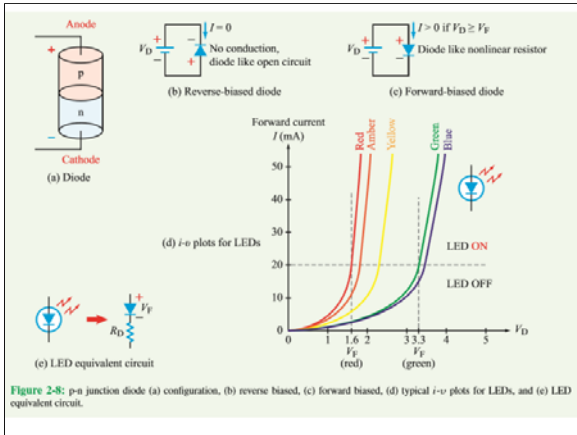
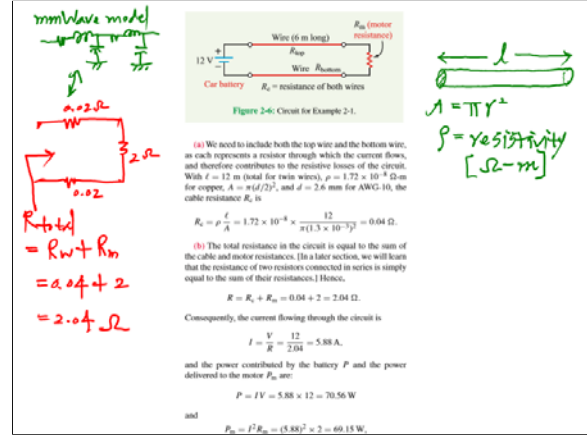
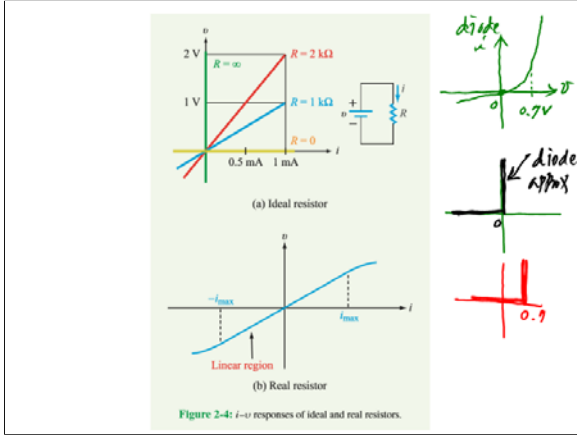
$$v = iR, \quad (2.3)$$

with the resistance  $R$  being the proportionality factor.

► In compliance with the passive sign convention, current enters a resistor at the "+" side of the voltage across it.

Ohm's Law:  $i = \frac{1}{R} v$   
 $v = R i$   
 $dW = R di$

An ideal *linear resistor* is one whose resistance  $R$  is constant and independent of the magnitude of the current flowing through it, in which case its  $i-v$  response is a straight line (Fig. 2-4(a)).



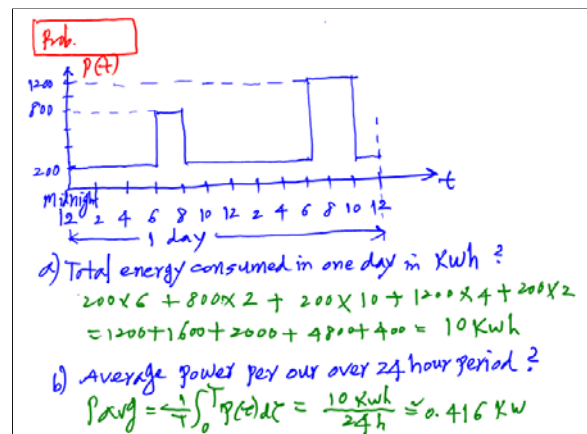
► A common convention is to assign a positive “+” sign to a current if it is entering the node and a negative “-” sign if it is leaving it. ◀

For the node in Fig. 2-9, the sum of currents entering the node is

$$i_1 - i_2 - i_3 + i_4 = 0, \quad (2.9)$$

where currents  $i_1$  and  $i_4$  were assigned positive signs because they are labeled in the figure as entering the node, and  $i_2$  and  $i_3$  were assigned negative signs because they are leaving the node.

► Alternatively, the sum of currents leaving a node is zero, in which case we assign a “+” to a current leaving the node and a “-” to a current entering it. ◀



**Prob.**

Find the total charge that passed through the element:

(a)  $t=1$  s, i.e.  $q(t=1)$   
 $q(t) = \int_0^t i(\tau) d\tau$   
 $q(0) = 0$   
 $q(1) = \int_0^1 10 d\tau = 10 \text{ A} \cdot 1 \text{ s} = 10 \text{ Coulomb [C]}$

(b)  $t=3$  s, i.e.  $q(t=3)$   
 $q(3) = \int_0^3 i(\tau) d\tau = 10 + 7.5 + 5 = 22.5 \text{ C}$

(c)  $t=5$  s, i.e.  $q(t=5)$   
 $q(5) = \int_0^5 i(\tau) d\tau = 22.5 + 7.5 = 30 \text{ C}$

**Prob.**

For  $t \geq 0$ ,  $v(t) = 10 \cos 2t$  [V],  $i(t) = 20(1 - e^{-0.5t})$  [mA]

a) Find the charge in the device at  $t = 2.5$   
 (assume initial charge at  $t=0$  is zero)  
 $e = 2.718$ ,  $e^{-1} = 0.368$   
 $q = \int_0^{2.5} i(\tau) d\tau = \int_0^{2.5} 20(1 - e^{-0.5\tau}) d\tau$  [mA · s]  
 $= 20 \left[ \tau - \frac{e^{-0.5\tau}}{-0.5} \right]_0^{2.5} = 20 \left[ 2.5 - \frac{e^{-1.25}}{-0.5} \right]$   
 $= 20 \left[ 2.5 + (0.368 \cdot 1) \cdot 2 \right] = 20(2 + 0.736) = 20(2.736) = 54.72 \text{ mC}$

b) The power consumed by the device at  $t = \pi/5$  mC  
 ( $e^{-\frac{\pi}{5}} = 0.208$ )  
 $P(t) = v(t) i(t) = 10 \cos(2t) \times 20(1 - e^{-0.5t})$   
 $= 200 \times 0.792 = 158.4 \text{ mW} = 0.1584 \text{ W}$

**Example 1.10**

What is the polarity?

Case A:  $V_x = 3V$  (Case B:  $V_x = -3V$ )

is already presented using a loop analysis. Let's try to find  $V_x$ . [This is called Nodal Analysis]

Current  $i_{2\Omega}$  [A] =  $\frac{[5 - V_x] [V]}{2 [\Omega]}$  [Ohm's Law]  $\frac{V}{R} = I$

$i_{4\Omega}$  [A] =  $\frac{3 - V_x [V]}{4 [\Omega]}$   $I = \frac{V}{R}$

$i_{8\Omega}$  [A] =  $\frac{V_x [V]}{8 [\Omega]}$

Also  $i_{2\Omega} + i_{4\Omega} = i_{8\Omega}$  [Based on Kirchhoff's Current Law]  $\sum I_k = 0$  at a node

$\frac{5 - V_x}{2} + \frac{3 - V_x}{4} = \frac{V_x}{8}$

$4(5 - V_x) + 2(3 - V_x) = V_x$

$20 + 6 - 4V_x - 2V_x = V_x$

$26 = 7V_x \Rightarrow V_x = \frac{26}{7} [V]$

$i_{2\Omega} = \frac{5 - \frac{26}{7}}{2} = \frac{9}{14} [A]$

$i_{4\Omega} = \frac{3 - \frac{26}{7}}{4} = -\frac{5}{28} [A]$   
 means in opposite direction

$i_{8\Omega} = \frac{\frac{26}{7}}{8} = \frac{13}{28} [A]$

$i_{8\Omega} = i_{2\Omega} + i_{4\Omega}$  (KCL ✓)

Also, power absorbed in  $2\Omega$ ,  $4\Omega$ ,  $8\Omega$  resistors are:

$2\Omega$  case:  $\frac{9}{14} \text{ A}$   
 $P_{2\Omega} = \left[ \left( 5 - \frac{26}{7} \right) [V] \right] \left[ \frac{9}{14} [A] \right]$   
 $= \frac{9}{7} [V] \times \frac{9}{14} [A] = \frac{81}{98} [W]$

$4\Omega$  case:  $\frac{26}{7} \text{ V}$   
 $P_{4\Omega} = \left( \frac{26}{7} - 3 \right) [V] \times \frac{5}{28} [A] = \frac{5}{7} \times \frac{5}{28} = \frac{25}{196} [W]$

$8\Omega$  case:  $\frac{26}{7} \text{ V}$   
 $P_{8\Omega} = \frac{26}{7} [V] \times \frac{13}{28} [A] = \frac{169}{98} [W]$

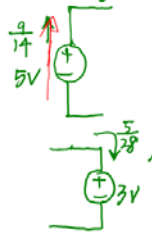
Total consumption

$$P_{\text{total}} = \frac{81}{98} + \frac{25}{196} + \frac{169}{98} = \frac{162 + 25 + 338}{196}$$

$$= \frac{525}{196} = \frac{25}{28} \text{ [W]}$$

*conservation (not zero)*

Power generated by two voltage sources:



$P_{5V} = -5[V] \times \frac{9}{14} = -\frac{45}{14}$

*negative sign since this is supplied*

$P_{3V} = +3[V] \times \frac{5}{28} [A] = +\frac{15}{28} [W]$

Total  $P_{5V} + P_{3V} = -\frac{45}{14} + \frac{15}{28} = -\frac{75}{28} [W]$